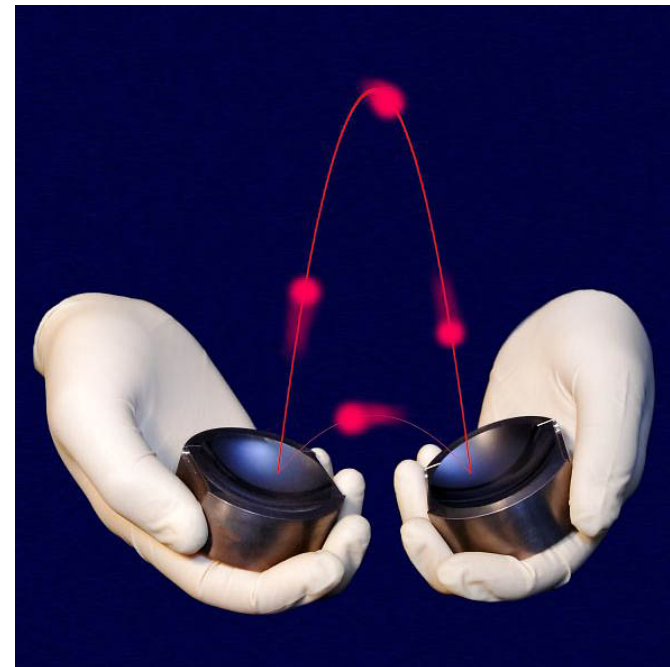


# Exploring the quantum with atoms and cavities

*J.M. Raimond*  
*Université Pierre et Marie Curie*

 **Laboratoire Kastler Brossel**  
 Physique quantique et applications

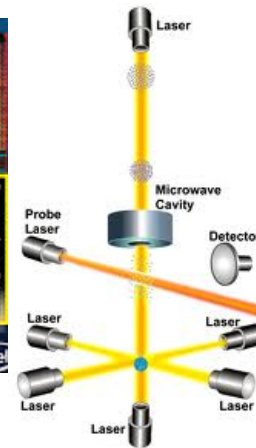
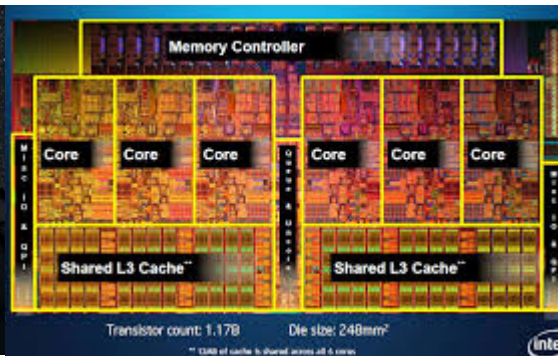


# Two radically different paths to explore quantum Nature

- The hard route
  - Constructing quantum (field) theory from first principles
- The quick and dirty experimental route
  - Look at quantum Nature at work
    - In situations simple enough to bring a direct insight into the most intimate quantum features.
  - No maths, a lot of plumbing, nuts and bolts
    - But some hopefully interesting questions to unveil and discuss
- At some point (« DEA Brossel », 39 years ago), Vincent and I chose to part on these two routes (being much older than me he chose the hard way...)
  - A splitting, which did not hamper a long-term friendship...
    - Happy birthday, Vincent !!

# A century of quantum physics

- A detailed understanding of the micro-world and...
  - Countless applications
    - Lasers, solid-state electronics, clocks, MRI...



## – A considerable societal and economic impact

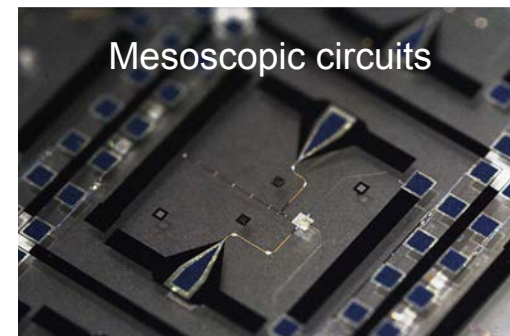
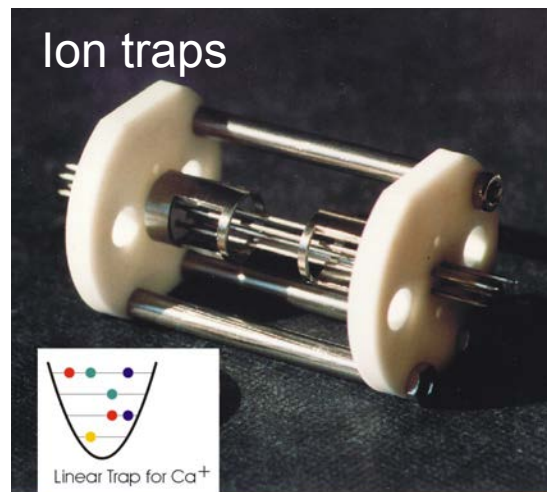
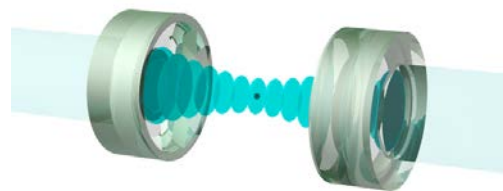
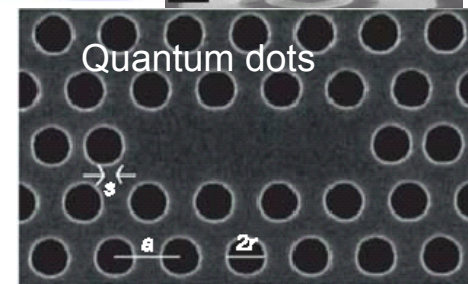
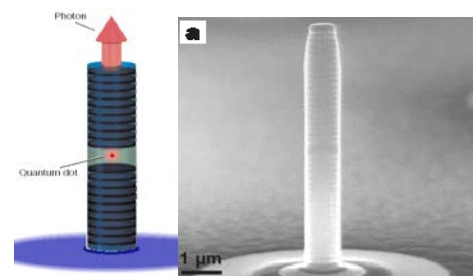
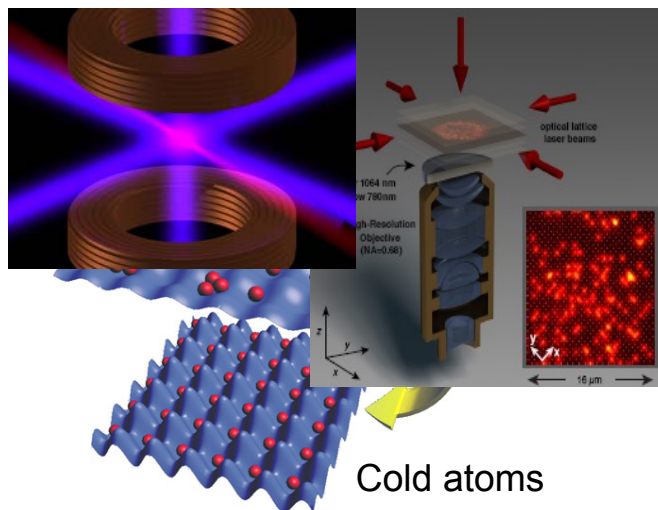
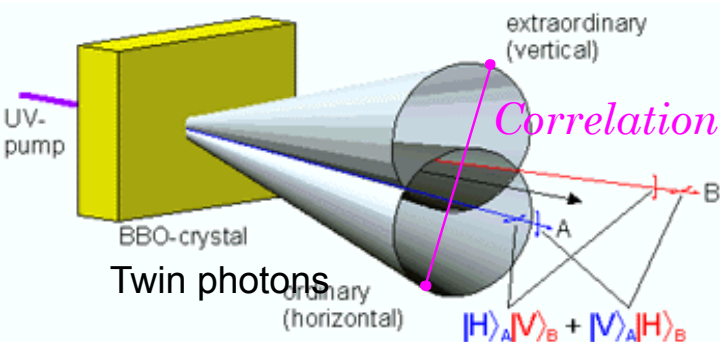
- Large part of GDP results from quantum technologies
  - Also large part of our lifetime expectation!
- No information society without the quantum
- An astounding example of the impact of curiosity-driven blue-sky research on the long term
  - Lessons for science support and granting system ?

# An unprecedented series of success...

- ...and provided us with extraordinary experimental tools
  - Lasers, computers allow us to manipulate quantum systems
    - Quantum technology makes it possible to explore the quantum.
    - The gedankenexperiments are made real
      - And quantum mechanics passes the test !
        - » What we do observe is precisely what the founding fathers extraordinary wits allowed them to predict
  - Why exploring the quantum 100 years after Bohr?
    - Better confidence in the quantum
    - Better understanding of the interpretation(s)
      - Measurement, state superpositions
    - Exploring the limits of the quantum
      - No quantum behaviors (superpositions aso) at our scale ?
    - Insights into new quantum technologies

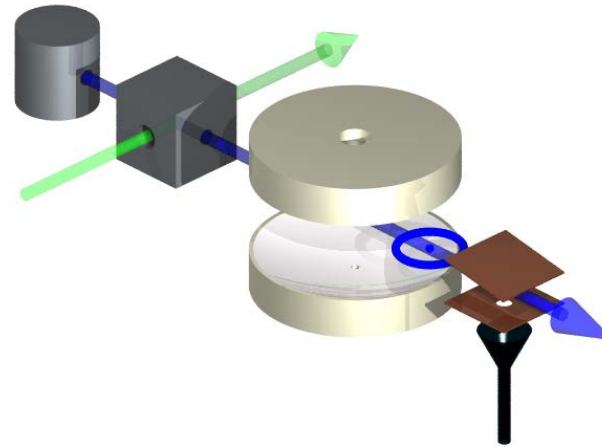
# A thriving field worldwide

- Many experimental schemes manipulate individual quantum systems



# Cavity Quantum Electrodynamics

- A spin and a spring



- **Realizes the simplest matter-field system:** a single atom coherently coupled to a few photons in a single mode of the radiation field, sustained by a high quality cavity.
- **Direct realization of thought experiments and illustrations of quantum postulates with circular Rydberg atoms and superconducting cavities**
  - Measurement
  - Complementarity
  - Macroscopic quantum superpositions (decoherence)

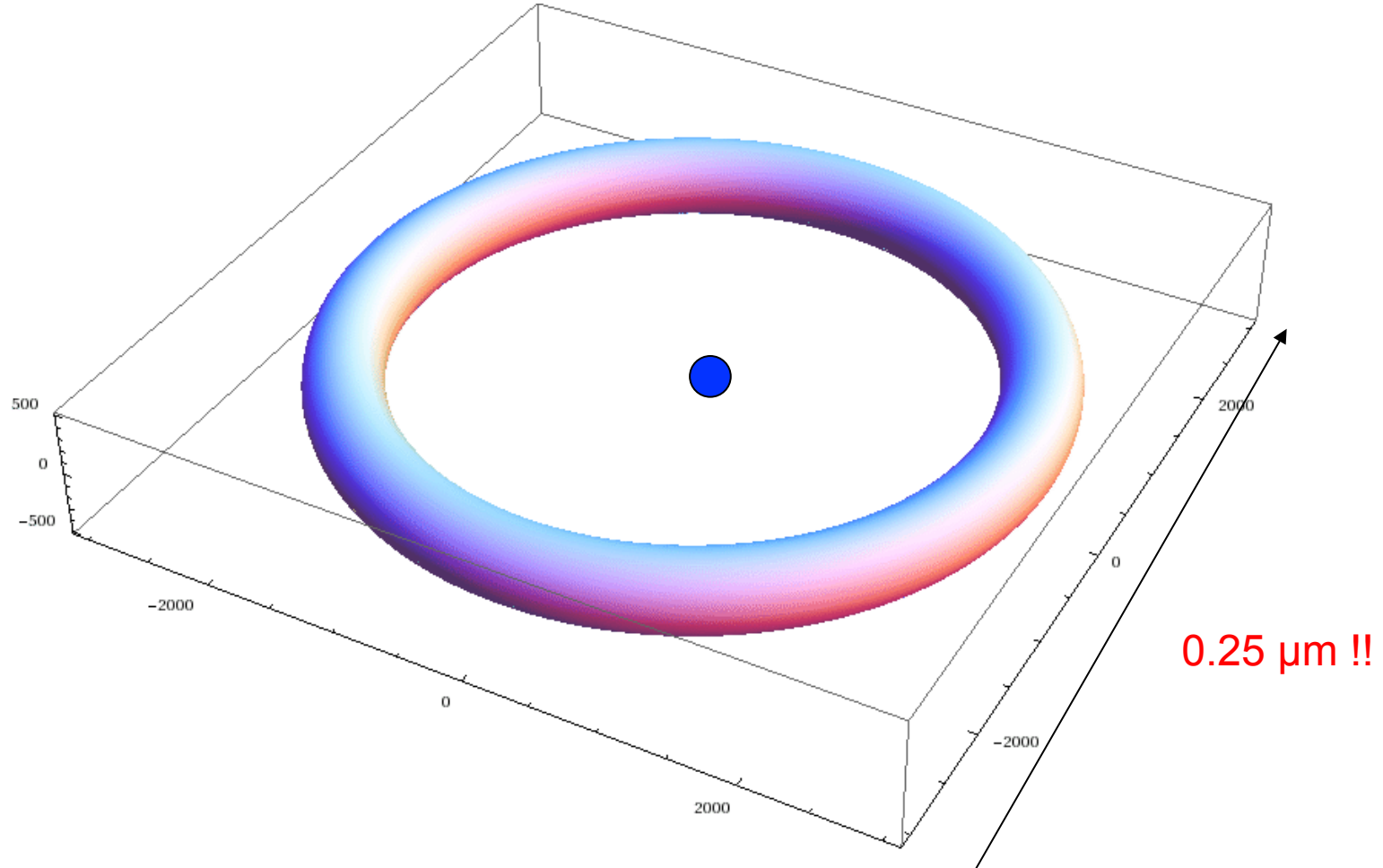
# A nearly ideal photon box

- Two mirrors
  - Separation 3 cm
    - Wavelength 6 mm, 51 GHz
  - Superconducting
    - No losses
    - Nearly perfect reflection
  - Photon lifetime  $T_c = 0.13\text{s}$  !
    - 1 billion bounces
    - 40000km
  - The best mirrors in the world



# Circular Rydberg states

- Giant atoms
  - Highly excited atomic levels

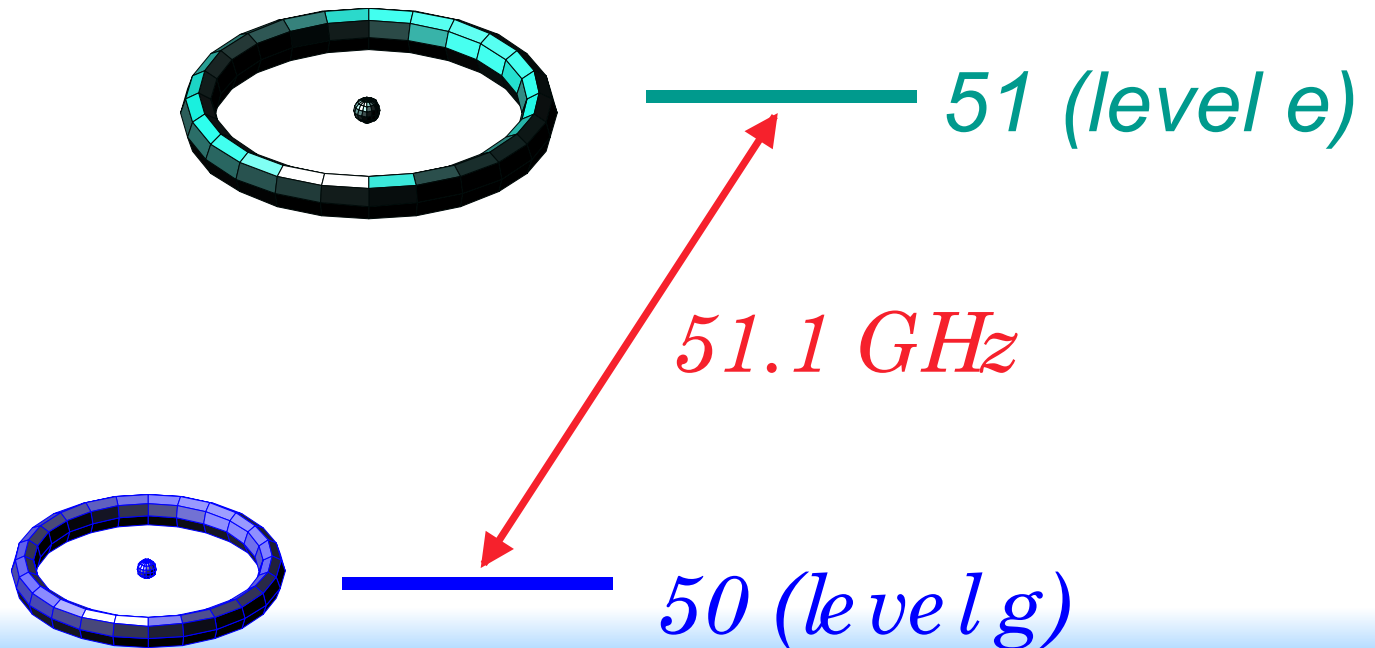


A ground state atom is 2500 times smaller !!



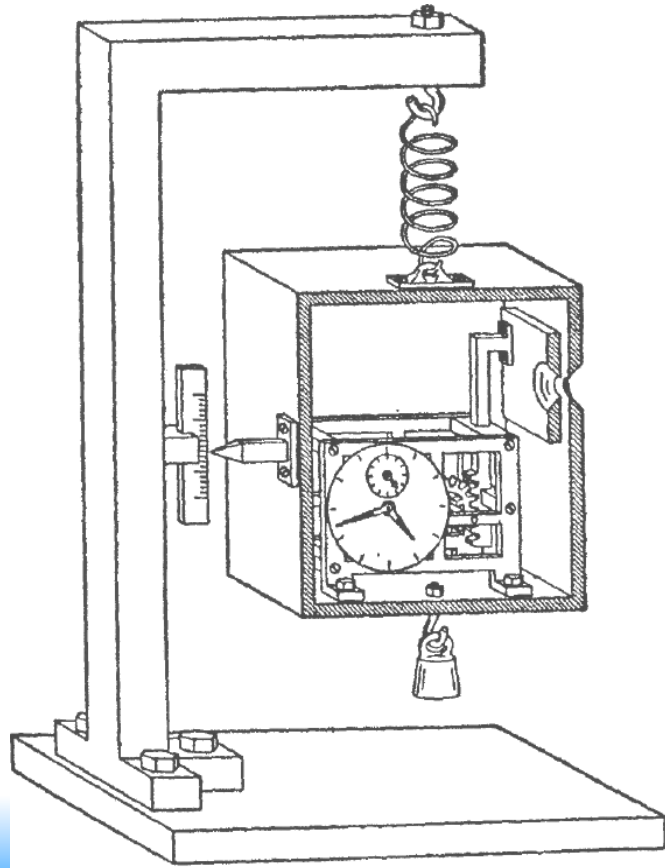
# Circular Rydberg states

- Ideal atoms
  - Long lifetime (30ms)
  - Strong coupling to the cavity field
  - Efficient state-selective detection
  - Some technicalities in the preparation stage

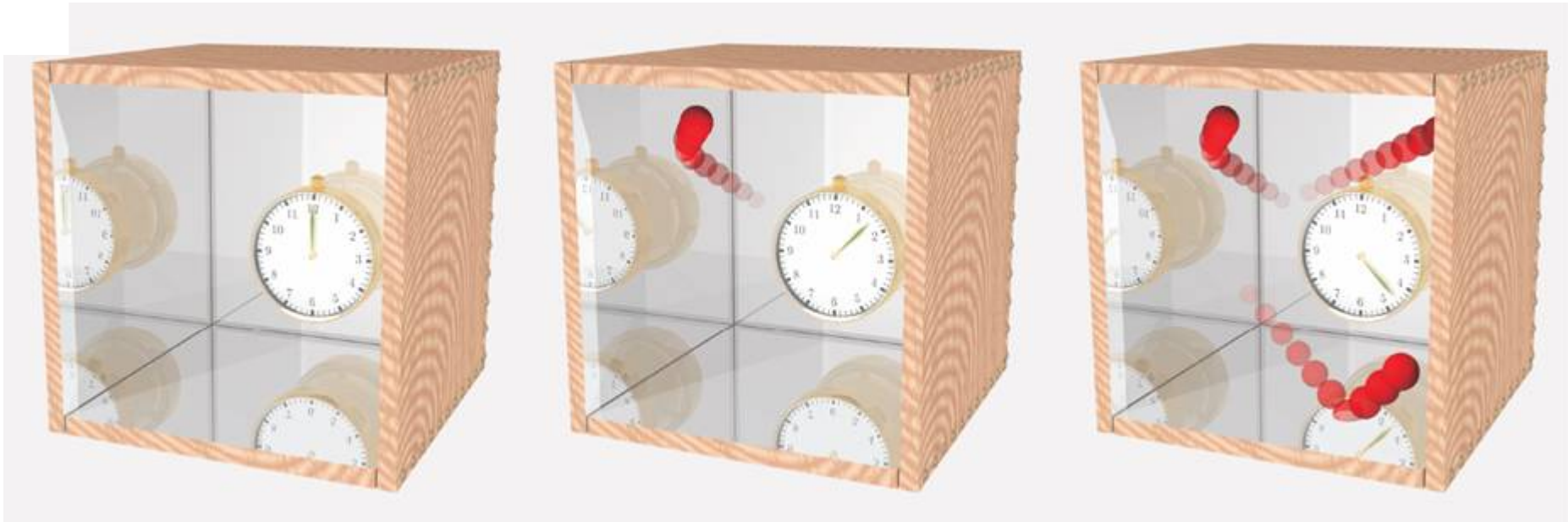


# An ideal photon counter ?

- All standard detectors destroy the incoming photons
  - A Quantum Non Demolition photodetector operating at the individual photon level
- A photon 'box' able to store a photon for a long time
  - back to Einstein-Bohr's dream: weighing a photon

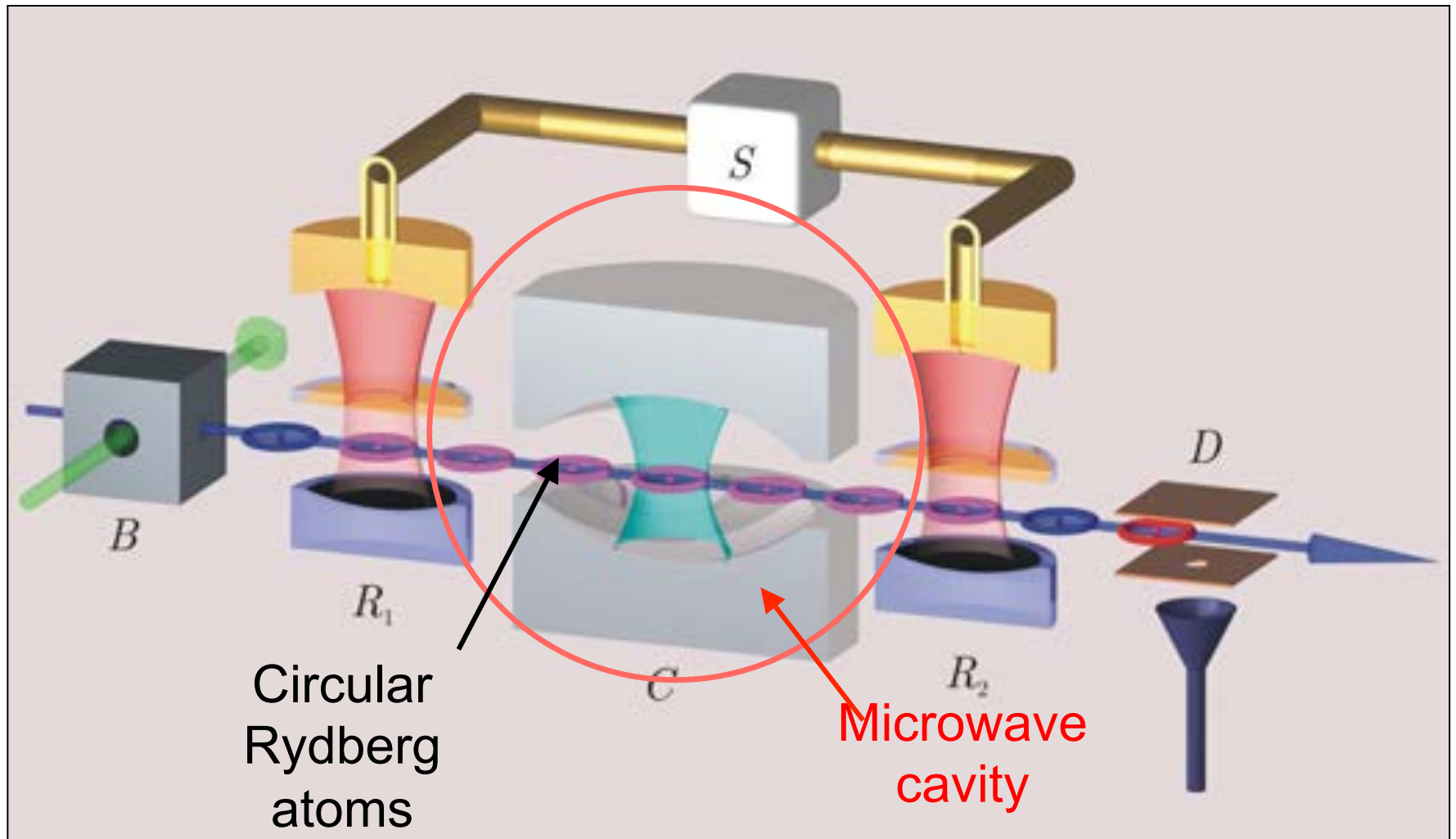


# Yet another gedankenexperiment

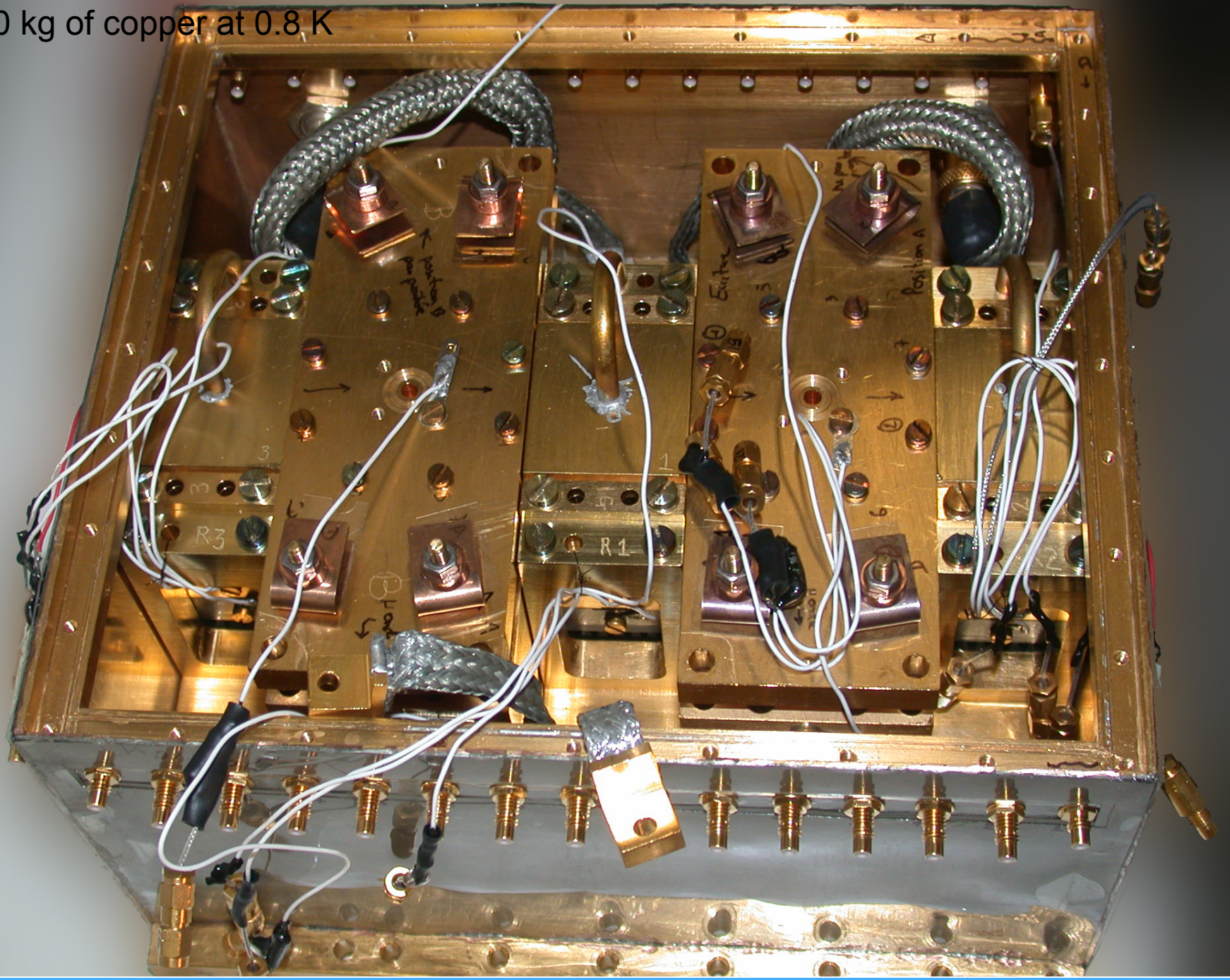


- A clock whose ticking rate is determined by the number of photons in a box
- The final clock hand's position directly measures the photon number
  - Photon box: a superconducting cavity
  - Clock: a single circular Rydberg atom

# Experimental set-up

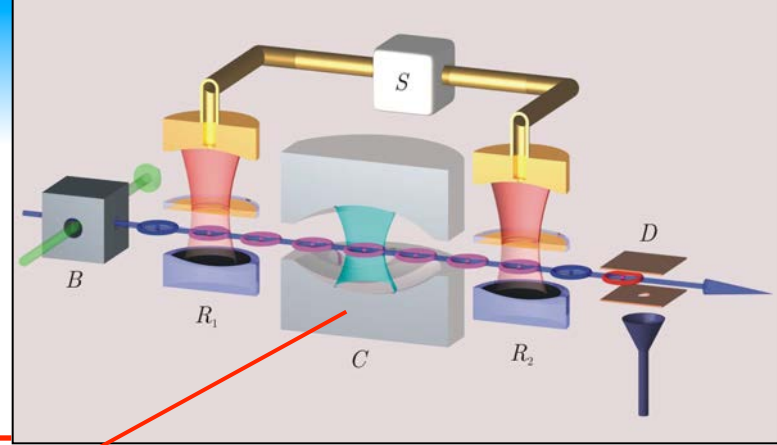
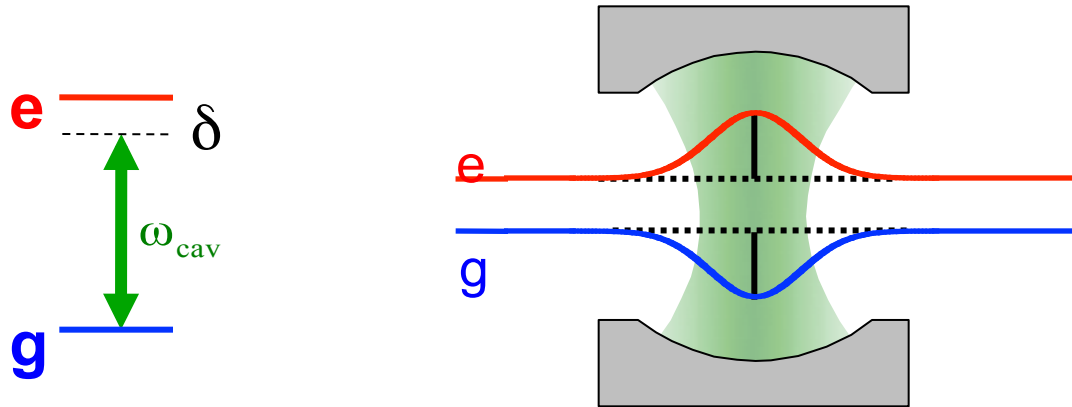


40 kg of copper at 0.8 K



# QND measurement

- Quantized light-shifts in the cavity

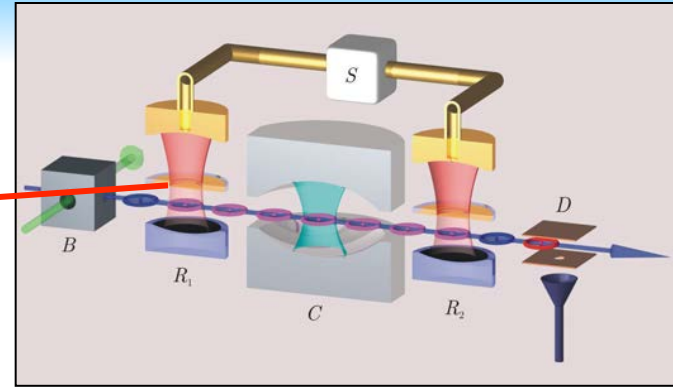


- Atomic clock modified by the interaction with the field
- Modification measured by Ramsey interferometry
  - A state superposition, prepared by a  $\pi/2$  pulse in  $R_1$ , accumulates a phase shift  $\phi_0 (n + 1 / 2)$
  - Phase shift read out by a second  $\pi/2$  pulse in  $R_2$  and final atomic state detection in D

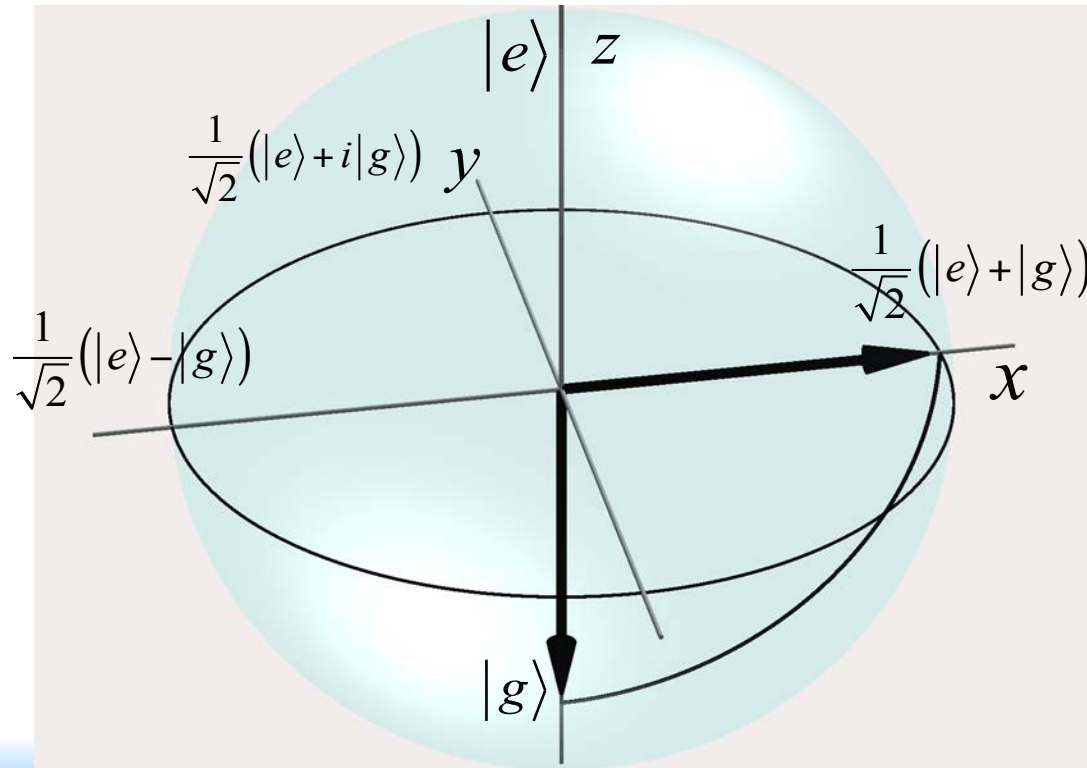
# Starting the clock

- Create an atomic coherence

- In  $R_1$  :  $|g\rangle \rightarrow \frac{1}{\sqrt{2}}(|g\rangle + |e\rangle)$

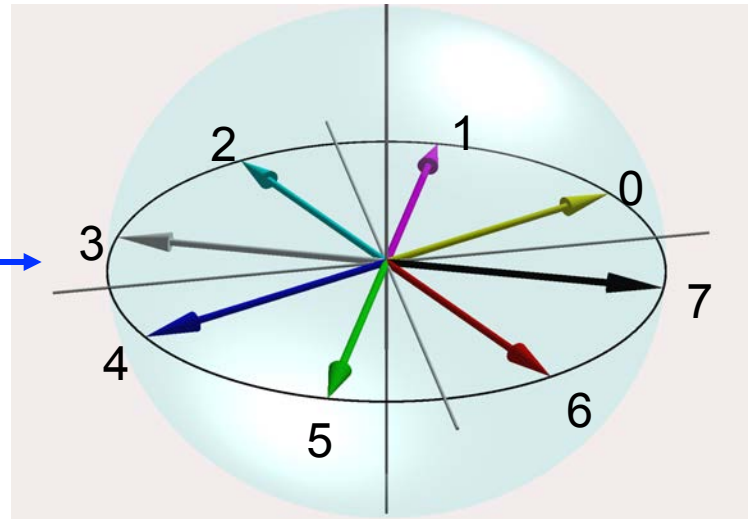
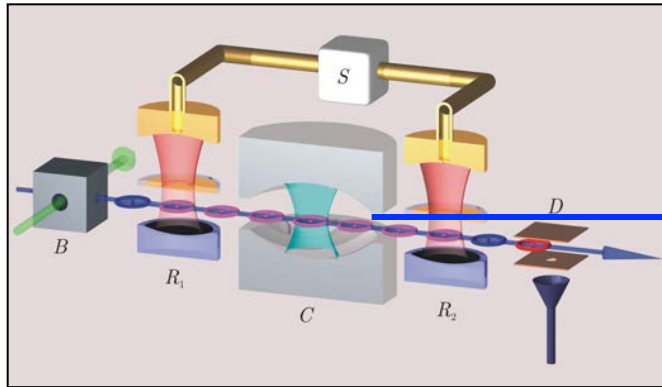


- **A simple geometrical representation:** Bloch sphere for the spin  $\frac{1}{2}$  representing the two-level atomic transition



# Quantized rotation of the atomic spin

- Photon-number dependent phase shift of the atomic coherence

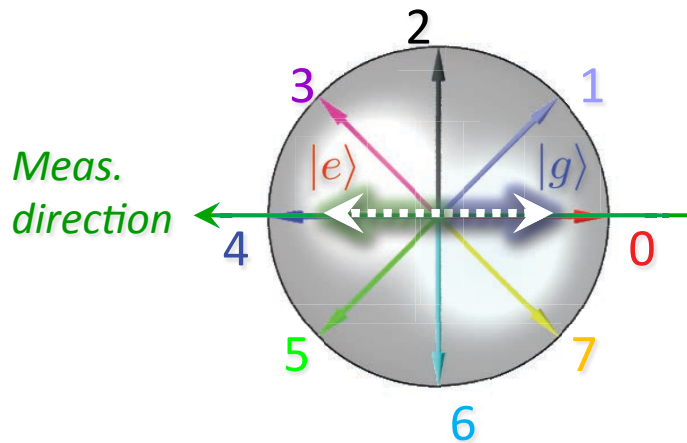


$$\phi_0 = \frac{\pi}{4}$$

- The Bloch vector direction reveals the photon number
- In general non-orthogonal final atomic states correspond to different photon numbers: **A single atom does not tell all the story**
- By choosing the phase of the pulse in  $R_2$ , measure the component of the spin in any direction of the equatorial plane



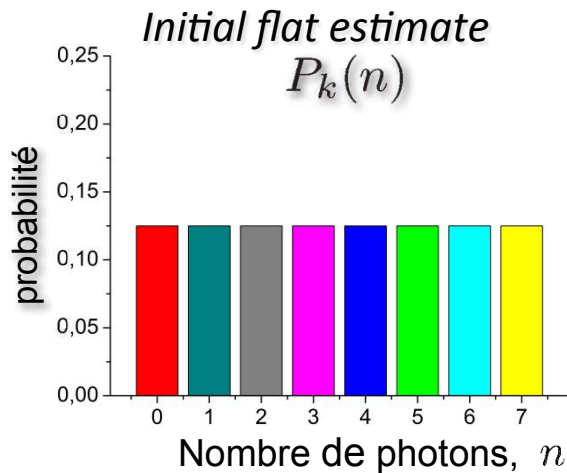
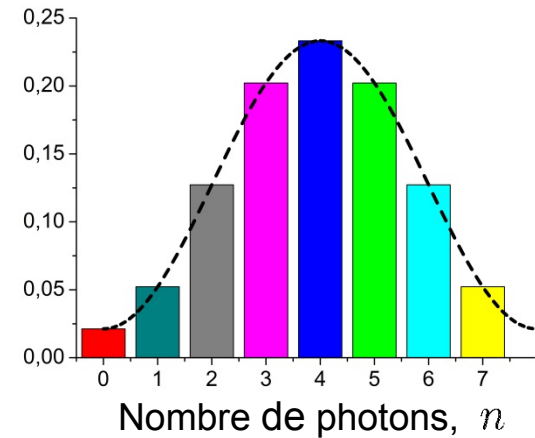
# Single atom detection



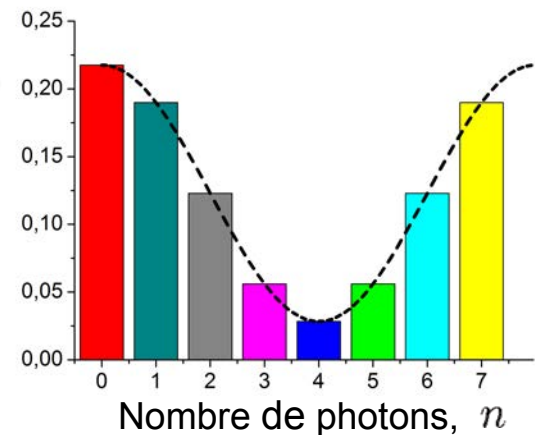
Each detection brings partial information on the photon number

$$P_{k+1}(n) \propto p(e|n)P_k(n)$$

detection  $|e\rangle$



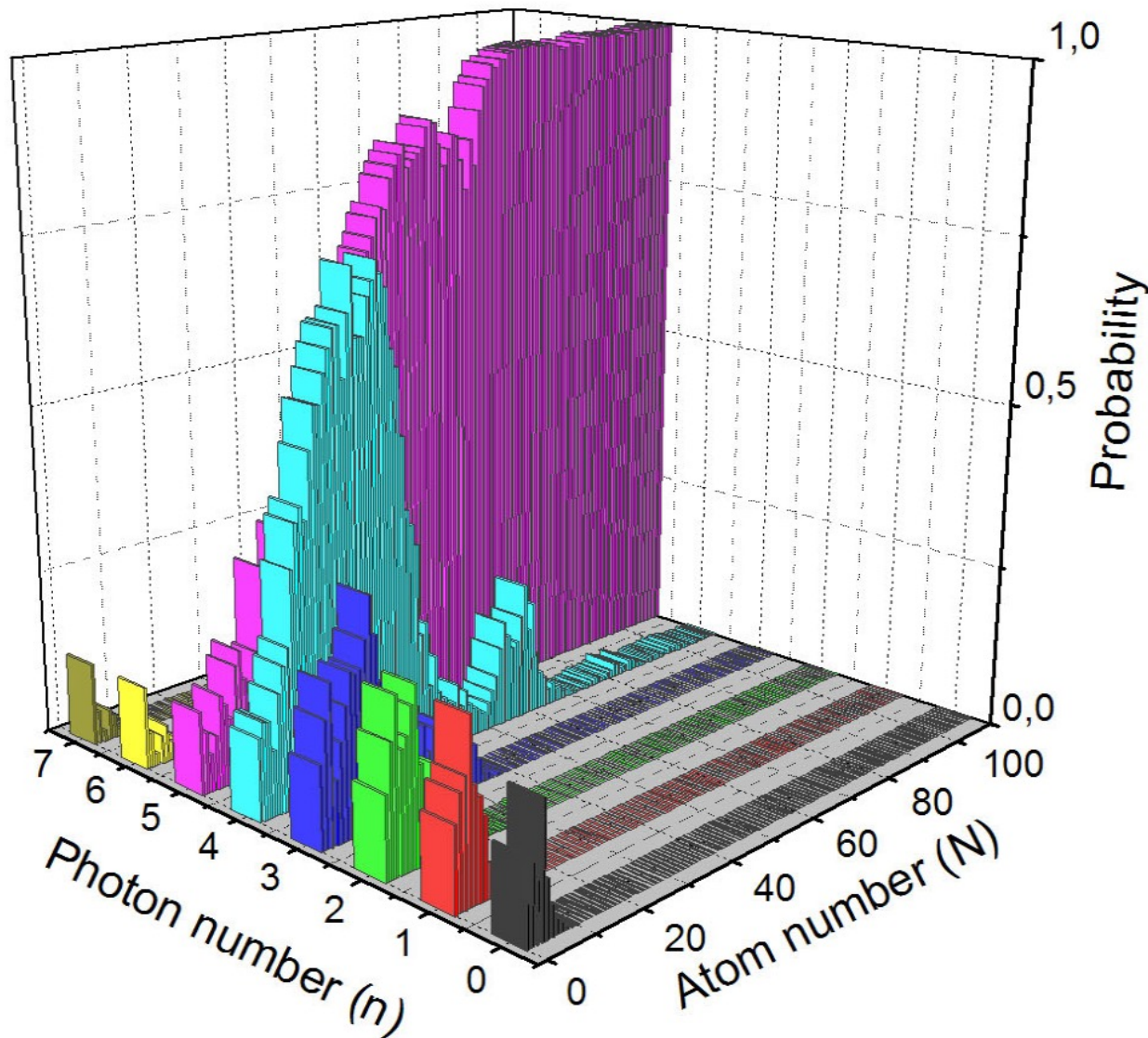
detection  $|g\rangle$



# Bayesian inference of the photon number distribution

- Each atom brings partial information on the photon number
  - Recording atomic state changes our inference of the photon number distribution  $P(n)$ 
    - $P(n)$  multiplied by a sine function after each atomic detection  
(probability to get the atom in the detected state as a function of the photon number)
      - Some photon numbers nearly ruled out
- Cumulative decimation of the photon number distribution pins down the photon number
  - Use four settings of the measurement direction chosen randomly
    - Removes any ambiguity and speeds up decimation
  - Requires about  $n_m^2$  atoms to distinguish  $n_m$  photon states
    - Statistical noise on the atomic detections

# Wave-function collapse in real time



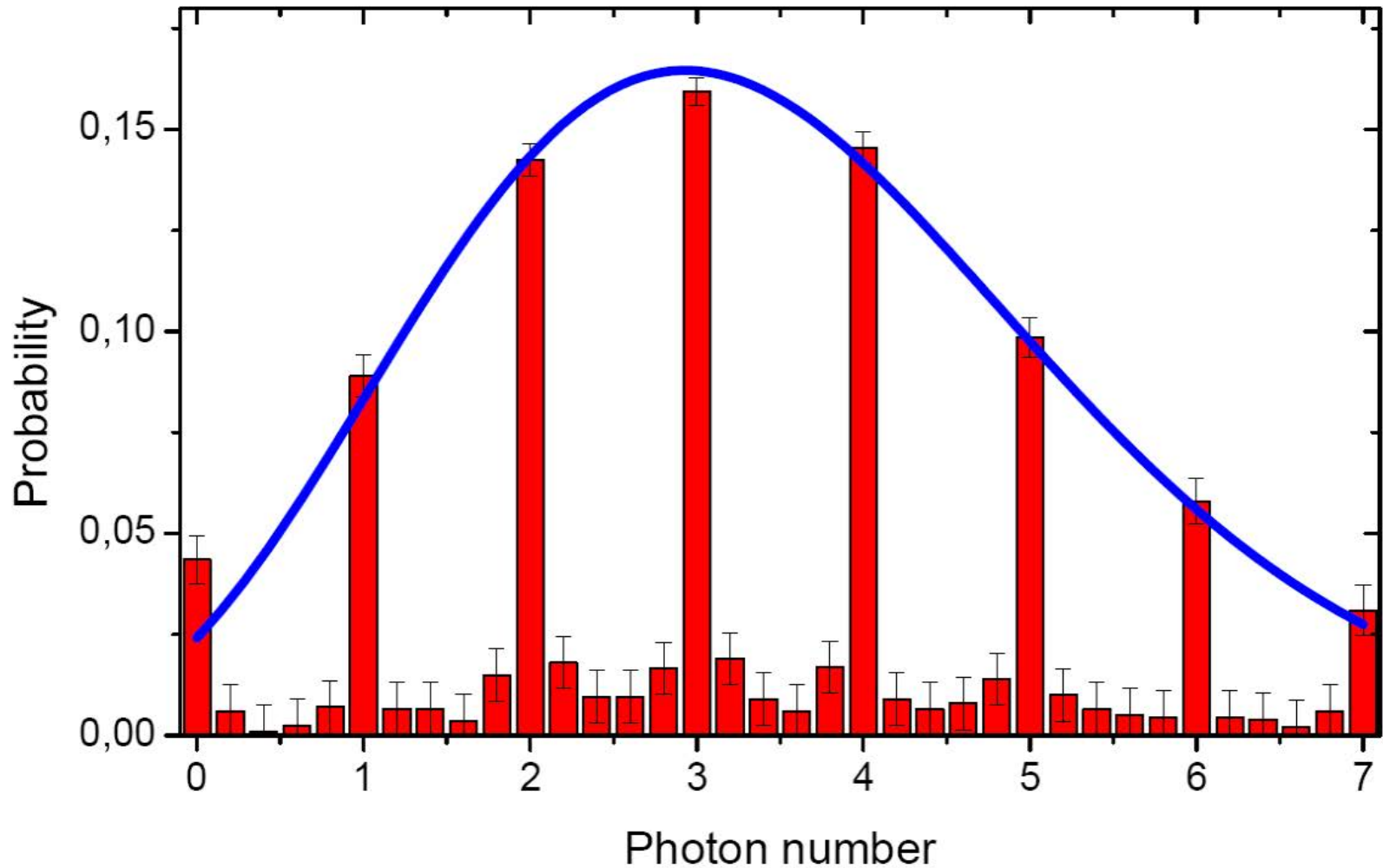
- Evolution of  $P(n)$  while detecting 110 atoms in a single sequence

- Initial coherent field with 3.7 photons

- Initial inferred distribution flat (no information) but final result independent of initial choice

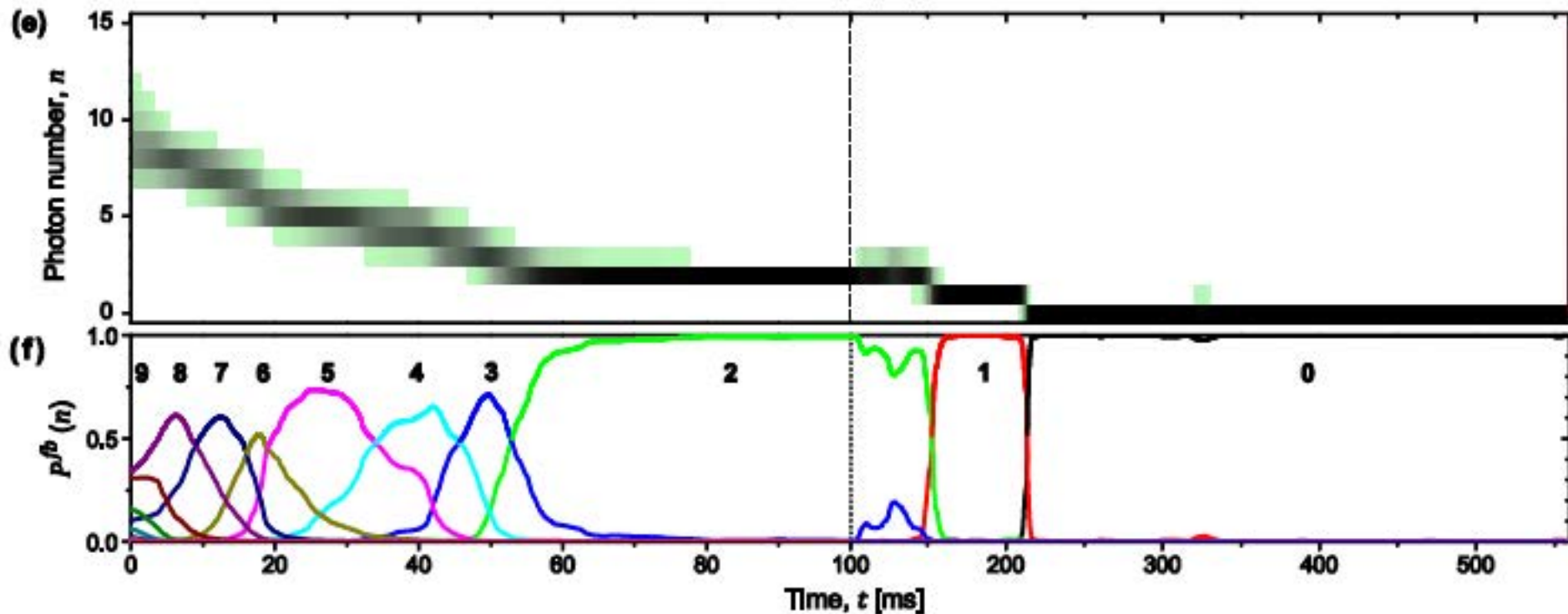
- Progressive collapse of the field state vector during information acquisition

# Photon number statistics



Excellent agreement with the expected Poisson distribution

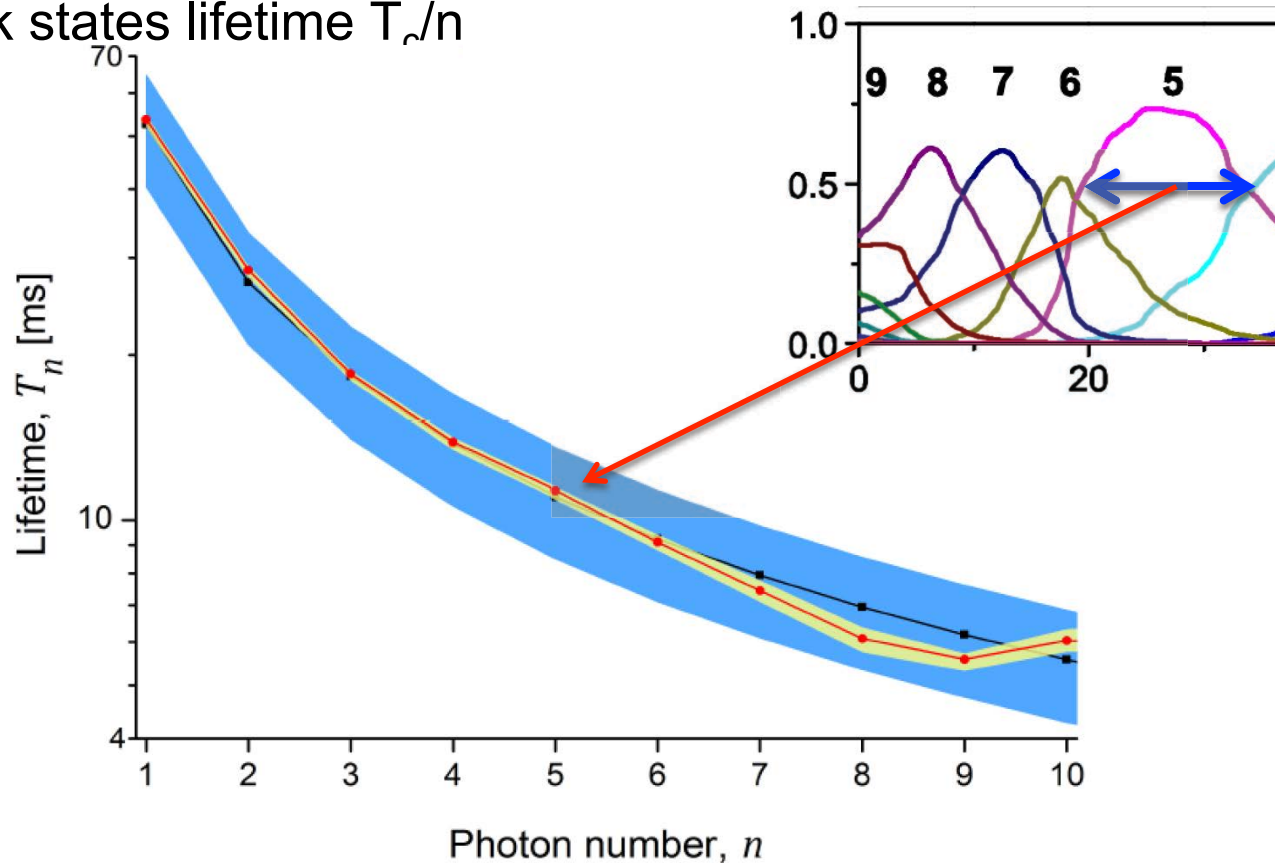
# Monitoring the light quantum jumps



- An improved analysis method based on the Past Quantum state formalism
  - Allows counting beyond the  $n=8$  periodicity
- Rapid decay of the higher Fock states

# Application: lifetime of the $n$ photon Fock state

- Analyze average time between jumps
  - Fock states lifetime  $T_n/n$



- Quantum states are fragile, all the more so when they get large:
  - decoherence

# Superpositions in the macro world ?

- The Schrödinger cat
  - No quantum superpositions at our scale

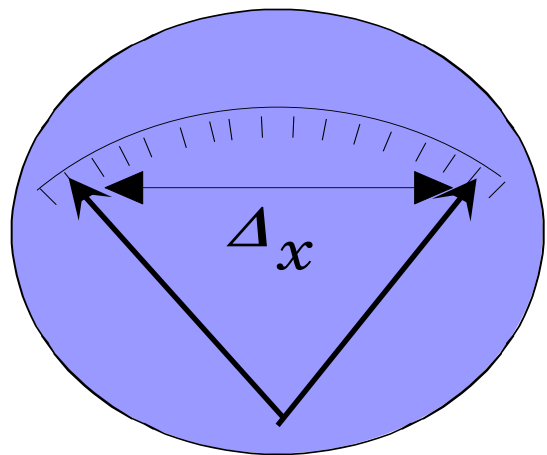
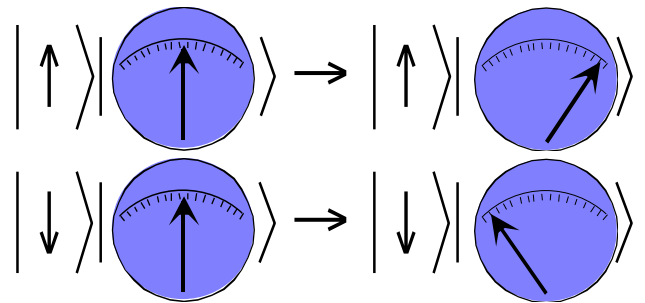


- We only observe a tiny fraction of all possible quantum states. Why ?

# Superposition, measurement and decoherence

- An essential question for quantum measurement
  - Linearity predicts measurement apparatus in a quantum superposition

- **High AND low**



$$\frac{1}{\sqrt{2}} (|\uparrow\rangle + |\downarrow\rangle) | \text{needle up} \rangle \rightarrow$$

$$\frac{1}{\sqrt{2}} (|\uparrow\rangle | \text{needle up} \rangle + |\downarrow\rangle | \text{needle down} \rangle)$$

$$\frac{1}{\sqrt{2}} (|\uparrow\rangle | \text{cat} \rangle + |\downarrow\rangle | \text{green} \rangle)$$

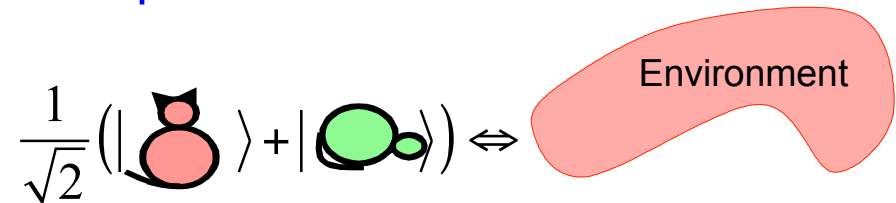
- Postulates predict a mixture (**high OR low**)
  - **The unlucky cat is a metaphore of measurement**



# Decoherence and quantum superpositions

- A quantum system is coupled to a complex environment

- Residual gas
- Residual radiation
- Gravity waves !



- Well controlled microsystems

- Coupling to environment negligible For All Practical Purposes

- Mesoscopic or macroscopic systems

- This coupling can NEVER be neglected
- Obviously the case for a measurement apparatus or a cat

# Decoherence models

- No general theory
- Simple cases in which quantum relaxation theory can be used to treat explicitly the coupling of a mesoscopic system with an environment
  - Brownian motion (Leggett)
  - Damping of a harmonic oscillator
  - ...
- Characteristics valid for all models
  - A few states are nearly stable (pointer states)
  - Their quantum superpositions are utterly unstable

# Pointer states

- Stable or nearly stable states in spite of environment coupling
  - Position states for Brownian motion
  - Vacuum for a zero temperature harmonic oscillator
  - Coherent field states
    - A coherent state remains coherent, its energy is damped as the classical field energy
  - All those states are exactly or almost insensitive to decoherence
- Quantum Darwinism
  - Pointer states are those who disseminate most easily copies of themselves into the environment without entanglement
  - All observers of a part of the environment can agree on which pointer state they 'observe'
    - Quantum objectivity (and realism)

# Mesoscopic quantum superpositions

- Pointer states superpositions
  - Rapidly transformed into a statistical mixture
    - One state OR the other instead of one state AND the other
  - Decoherence time scale
    - Short compared to the classical (energy) damping time
    - Shorter and shorter when the 'distance' between state increases.
  - An essential character of mesoscopic systems relaxation:
    - Two (very) distinct time scales
      - Slow one: energy
      - Fast one: decoherence
      - Their ratio is a good measure of the superposed state 'macroscopicity'

# Decoherence and quantum measurement

- Two essential ingredients
  - Measurement result is described by a classical probabilistic alternative
    - Same nature as that of statistical physics
    - God IS playing dice, but He is playing with classical dice
  - Decoherence defines the measured quantity
    - Final state: mixture of pointer states
      - The measured system's state are those correlated to pointer states
      - Without decoherence: entangled state of the system with the meter which can be cast in any joint basis
      - System-meter coupling AND decoherence dynamics both define the measured quantity.

# Experimental exploration of decoherence?

- Easy !
  - No quantum superpositions in everyday world...
- Not that simple ?
  - Resolve dynamics for a mesoscopic system (two well separated time scales) weakly coupled to its environment.
  - Long relaxation time so that decoherence time is long enough to be measured
  - Delicate probe of the system's state
- Few appropriate systems. Particularly:
  - Ion in traps
  - CQED

# Mesoscopic coherent fields in cavity QED

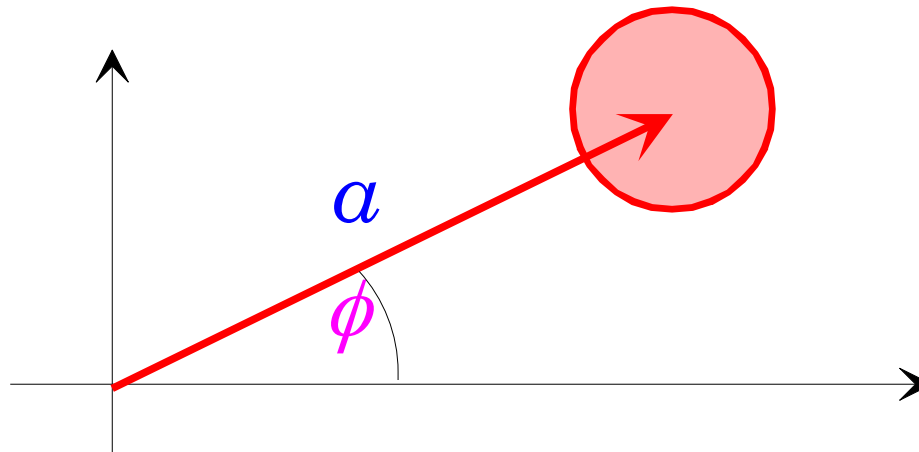
- A classical amplitude and quantum fluctuations

- Small field:



- A single photon coherent field is quite quantum: fluctuations as large as the amplitude

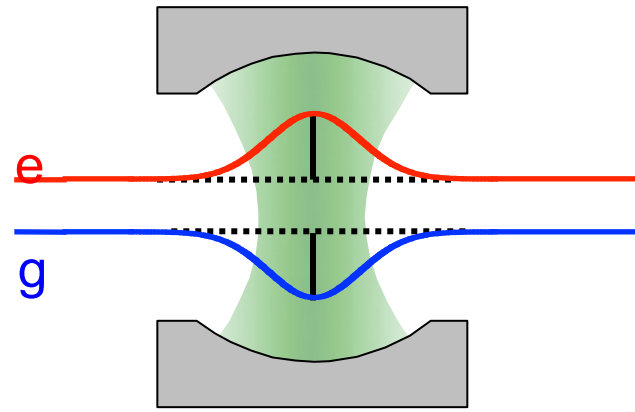
- Large field:



- A large coherent state is nearly classical

# Dispersive atom-field interaction

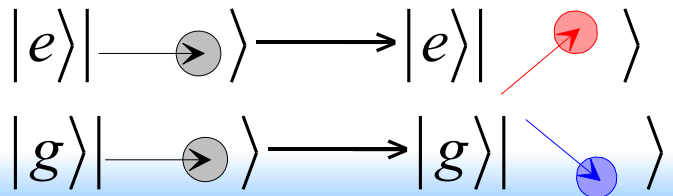
- Non resonant (dispersive) case
  - Two complementary effects
    - Atomic frequency modified by the cavity field (light shifts, proportional to the photon number)



– Phase of an atomic superposition changed

- Field frequency modified by the presence of the atom (index effect)

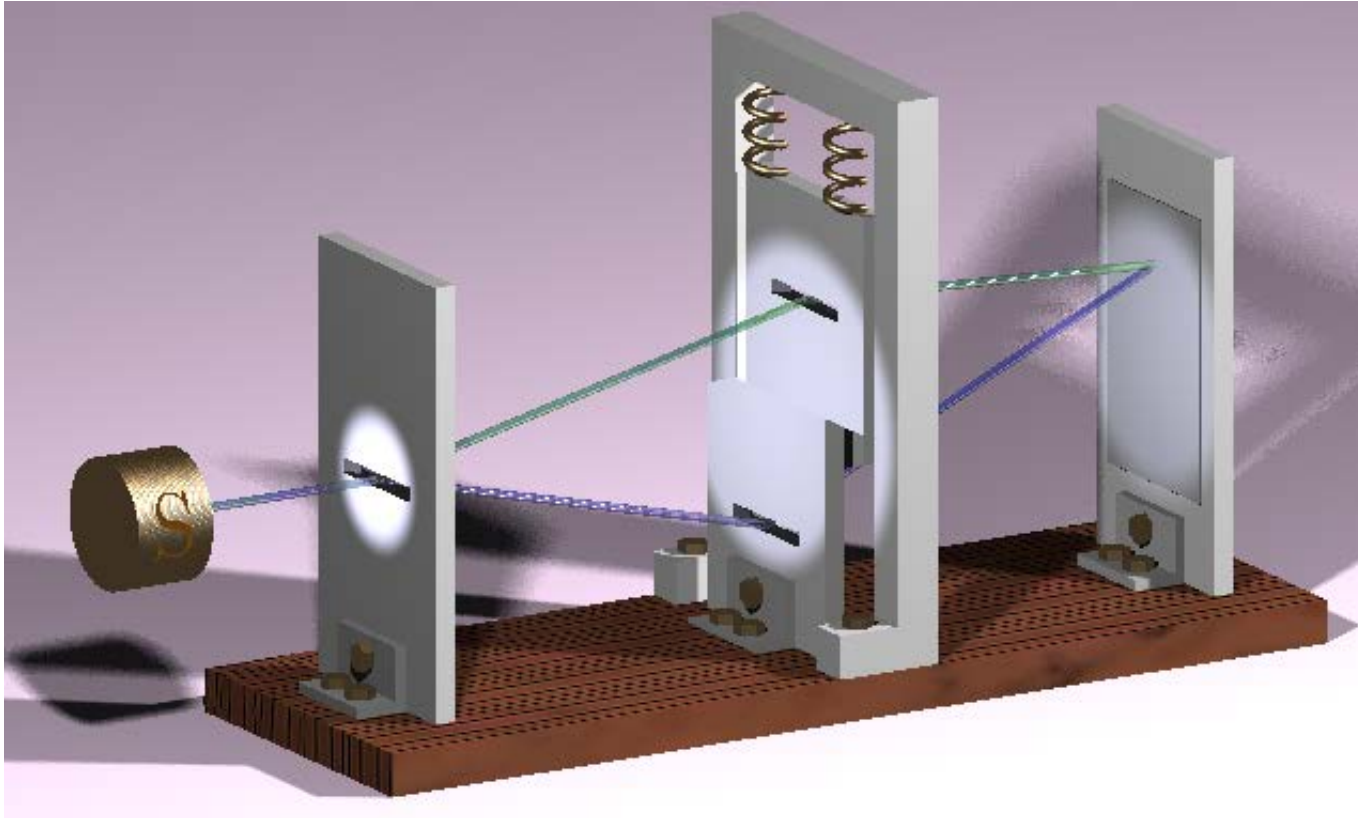
– Classical phase of the field changed (in a way depending upon the atomic state)





# Bohr's thought experiment on complementarity

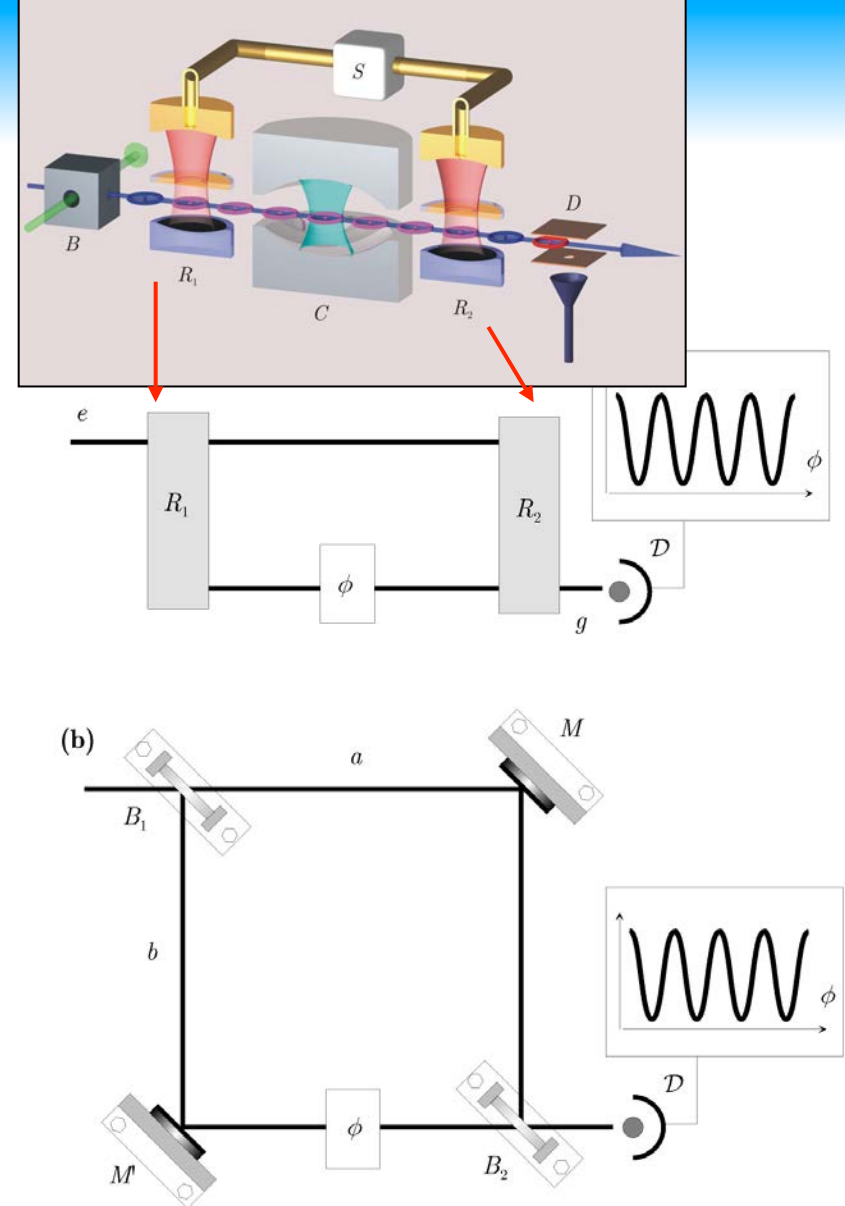
- **Complementarity** (From Einstein-Bohr at the 1927 Solvay congress)



- Moving slit records the trajectory of the particle in the interferometer

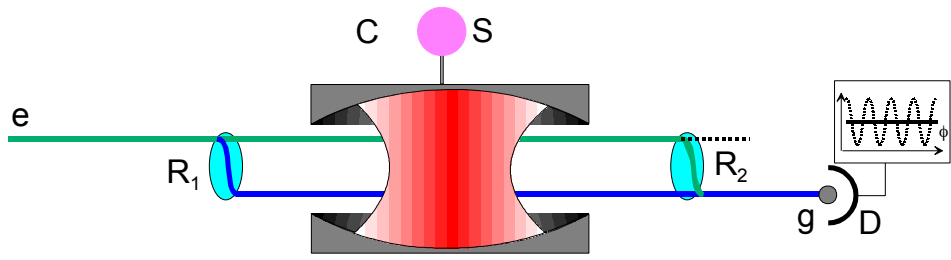
# Ramsey interferometer

- An atomic version of the Mach-Zehnder interferometer
  - Two classical resonant pulses mix atomic levels
    - Quantum interference
  - Transfer probability sinusoidal function of the phase accumulated by the atom

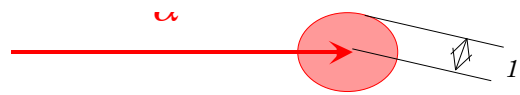


# Cavity field as a which path detector

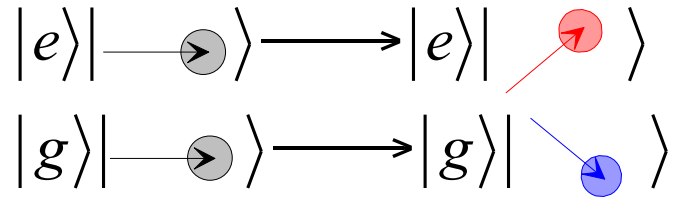
- Insert non-resonant cavity inside the Ramsey interferometer



- Cavity contains initially a mesoscopic coherent field



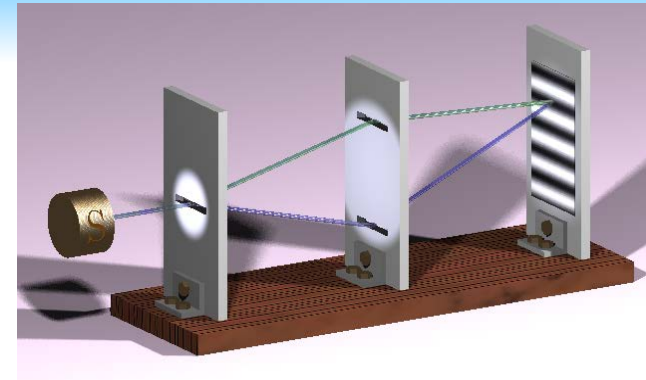
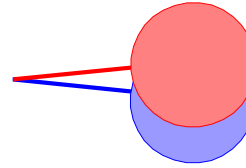
- The two atomic levels produce opposite phase shifts of the cavity field



- Field amplitude is the ‘needle’ of a ‘meter’ pointing towards atomic state
  - Prototype of a quantum measurement
  - Provides a which-path information and should erase the fringes

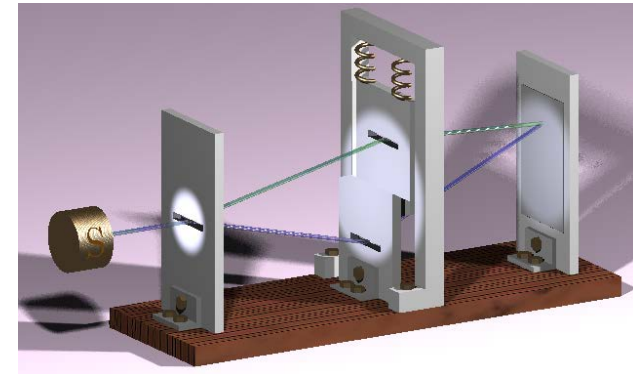
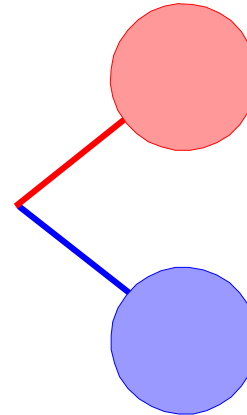
# Two limiting cases

- Small phase shift (large  $D$ )  
(smaller than quantum phase noise)



- field phase almost unchanged
- No which path information
- **Standard Ramsey fringes**

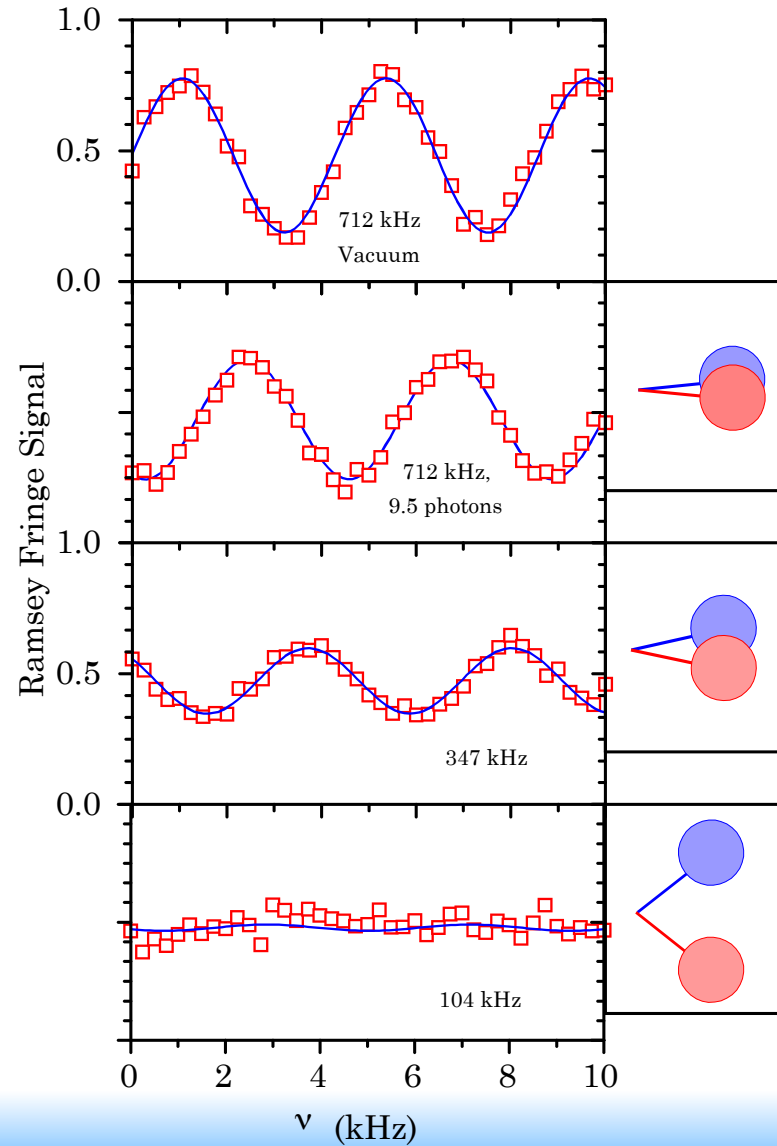
- Large phase shift (small  $D$ )  
(larger than quantum phase noise)



- Cavity fields associated to the two paths distinguishable
- Unambiguous which path information
- **No Ramsey fringes**

# Fringes and field state

- An illustration of complementarity



Brune et al. PRL 77, 4887

# A laboratory version of the Schrödinger cat

Field state after atomic detection

$$\frac{1}{\sqrt{2}}(|\nearrow\rangle + |\searrow\rangle)$$

A coherent superposition of two "classical" states.

Very similar to the Schrödinger cat



Decoherence transforms this superposition into a statistical mixture

time scale  $2T_c/D^2$  where  $D^2$  is the square distance between classical amplitudes  
(a photon number)

Slow relaxation time scale  $T_c$ : possible to study the decoherence dynamics

Decoherence caught in the act

# More insight into the quantum nature of a cat

- Prepare a cat by dispersive interaction with a single atom
- Wait...
- ... and see : reconstruct the field density matrix
  - Controlled displacements
  - QND photon number measurements
  - MaxEnt reconstruction algorithm
- Plot the cat's Wigner function

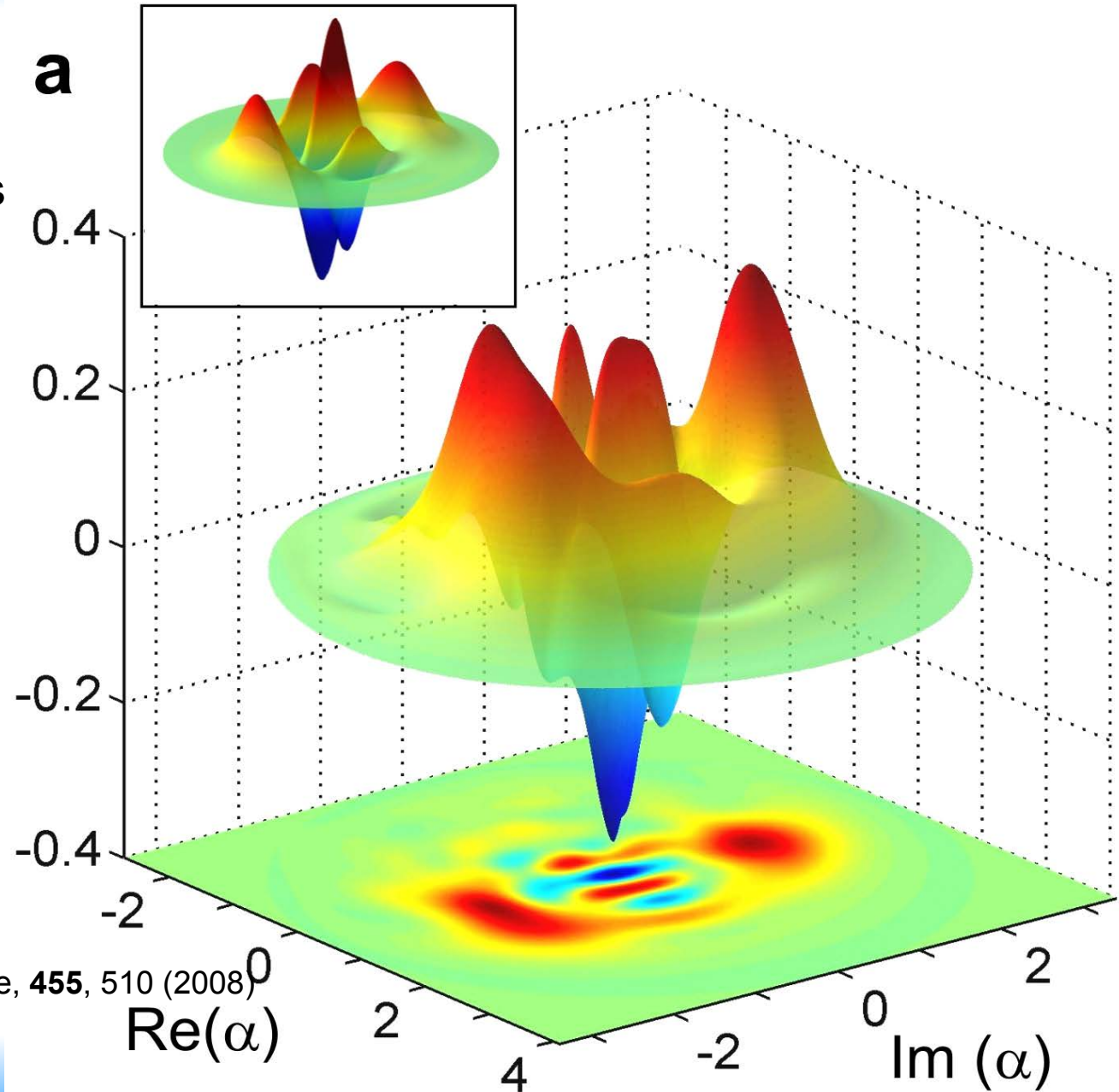
# The portrait of a cat

- Even cat

- $n=3.5$  photons

- $\zeta=0.37\pi$

- $D^2=11.8$   
photons

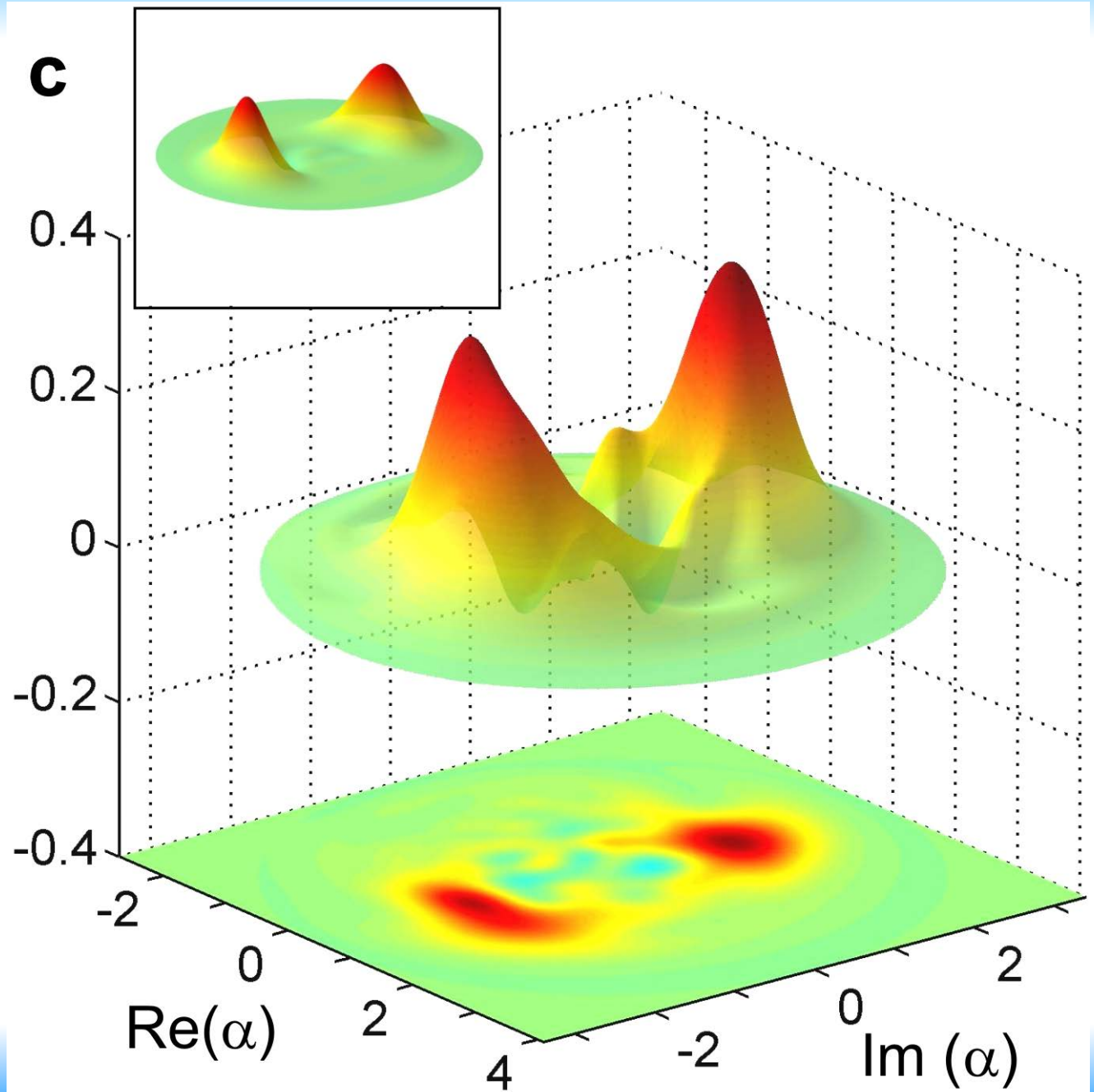


S. Deléglise et al, Nature, **455**, 510 (2008)



# Schrödinger cat states

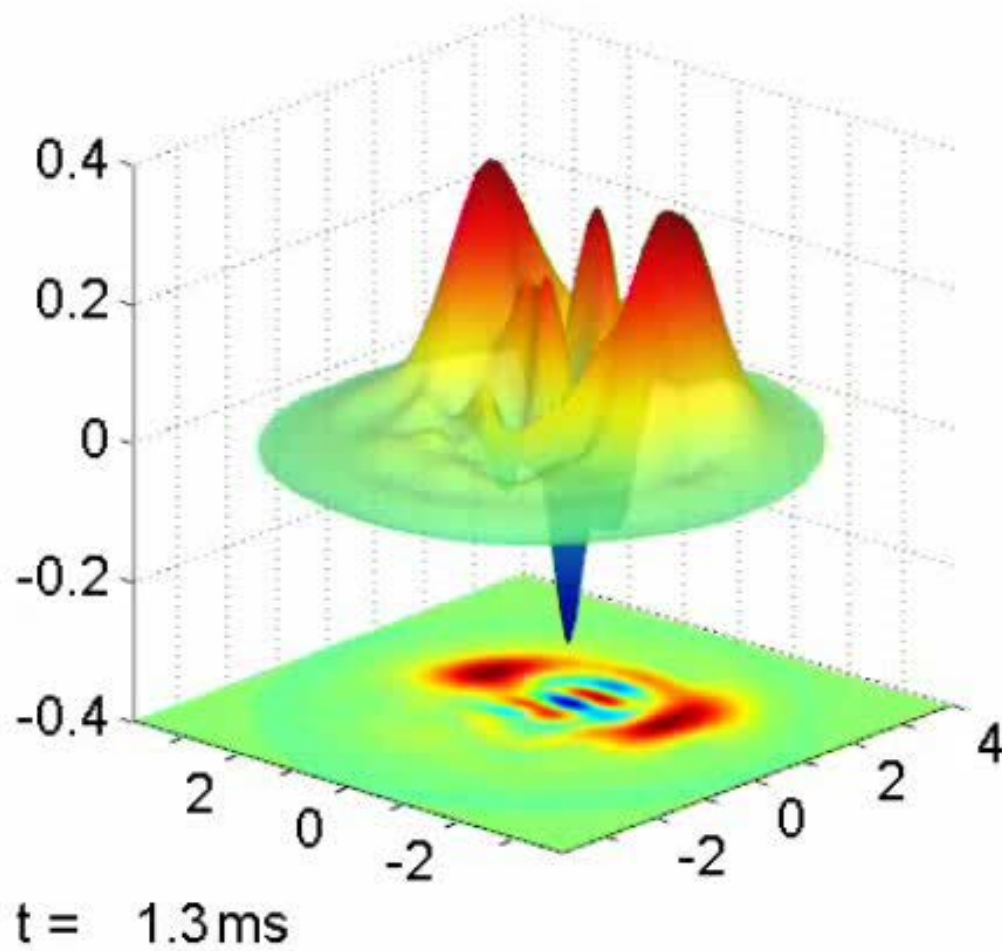
- Statistical mixture



# Decoherence of the cat

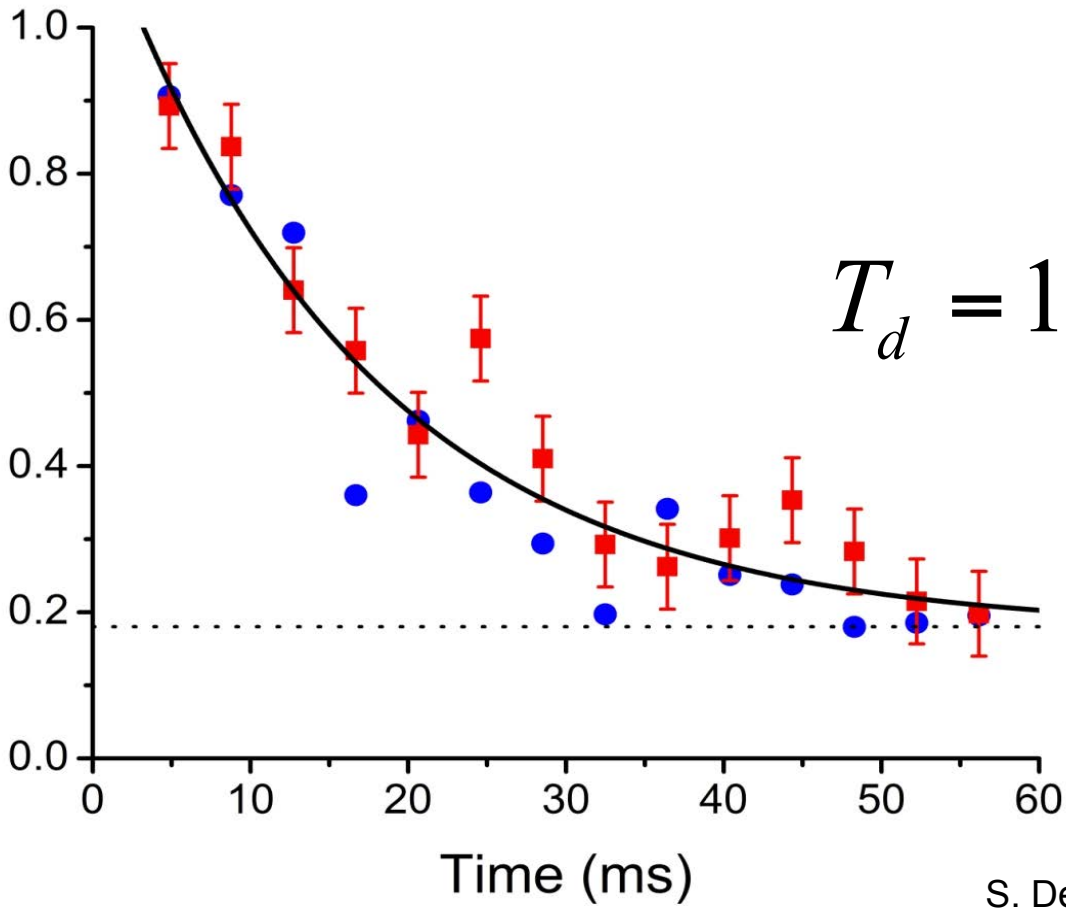
- Time resolved method
  - Data acquisition time: 4 ms
  - Much shorter than the expected decoherence time
    - 19 ms taking residual thermal effects into account
- Monitor cat decoherence in real time

# A movie of the cat decoherence



S. Deléglise et al, Nature, **455**, 510 (2008)

# Decoherence time



S. Deléglise et al, Nature, **455**, 510 (2008)

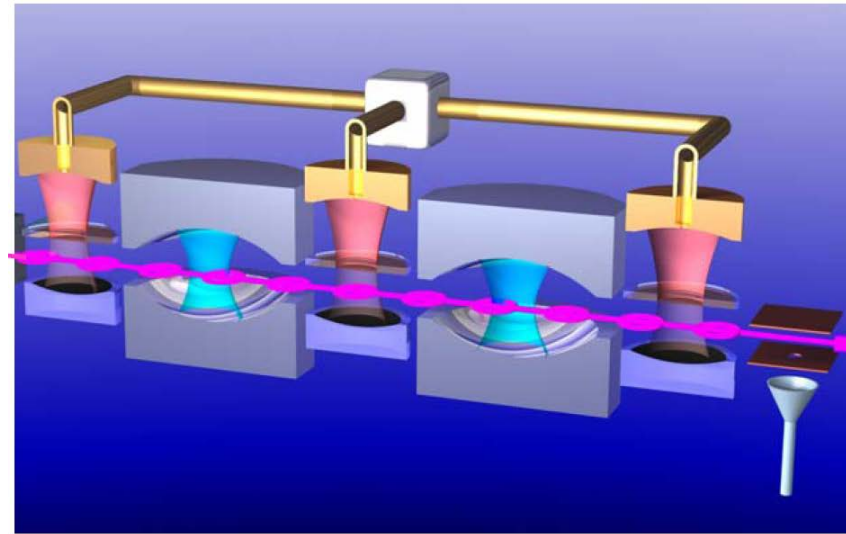
For similar work in circuit QED see Wang et al. PRL **103** 200404

# Conclusion: interrelated concepts

- Complementarity, decoherence and entanglement
  - No quantum interference when entanglement with a which path detector
  - No quantum interference for macroscopic objects
    - Decoherence
    - Results from an unavoidable entanglement with the environment.
  - And quantum superposition is at the heart

# Perspectives : A new breed of quantum monster

- Entangling a single atom with two mesoscopic fields



- Dispersive interaction:

no energy exchange but entanglement of the field classical phase with the atomic state (index of refraction)

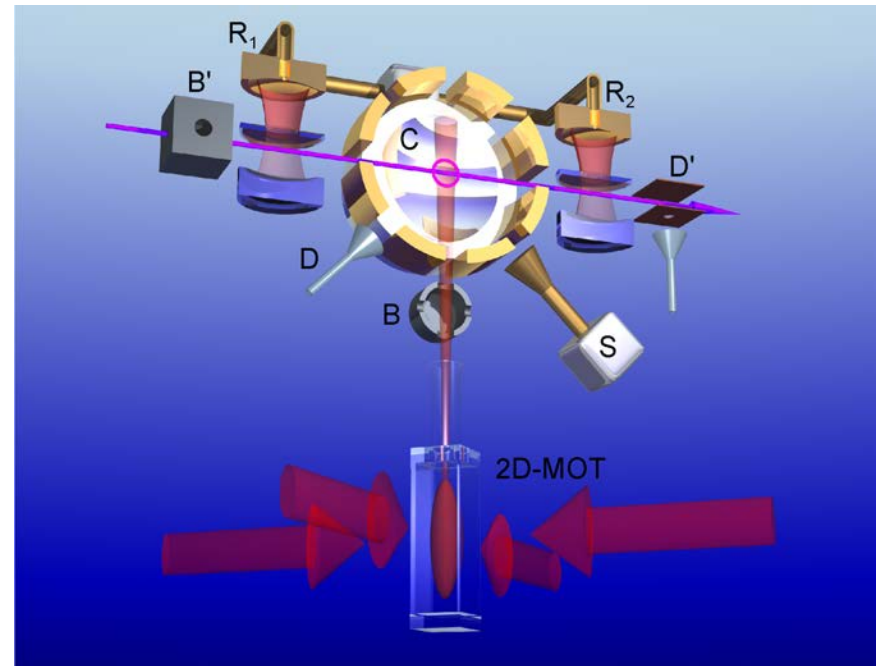
Final two-cavity state  $|\gamma, \gamma\rangle + |-\gamma, -\gamma\rangle$

P. Milman et al EPJD, **32**, 233

a non local mesoscopic quantum state

# Perspectives : Slow atoms in a cavity

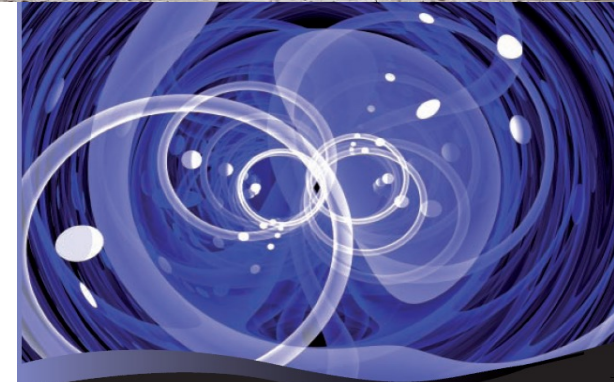
- A strong limitation of present experiments
  - Atom-cavity interaction time  $\ll$  both systems lifetime
    - $100 \mu\text{s} \ll 30\text{ms}, 0.13 \text{ s}$
- Achieving long interaction times
  - A set-up with a stationary Rydberg atom in a cavity
    - Circular state preparation and detection in the cavity
    - Interaction time ms range
    - Large cats
    - Quantum Zeno dynamics



J.M. Raimond et al PRL **105**, 213601

# A team work

- S. Haroche, M. Brune, J.M. Raimond, S. Gleyzes, I. Dotsenko, C. Sayrin
- Cavity QED experiments
  - S. Gerlich
    - T. Rybarczyk, A. Signoles, A. Facon, D. Grosso, E.K. Dietsche, V. Métilon, F. Assemat
- Superconducting atom chip
  - Thanh Long Nguyen, T. Cantat-Moltrecht
  - R. Cortinas
- Collaborations:
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    - CEA Saclay (DAPNIA)
  - Feedback: P. Rouchon, M. Mirrahimi, A. Sarlette
    - Ecole des Mines Paris
  - QZD: P. Facchi, S. Pascazio
    - Uni. Bari and INFN
- €€:ERC (Declic), EC (SIQS, RYSQ),
  - CNRS, UMPC, ENS, CdF



## Exploring the Quantum

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Serge Haroche and  
Jean-Michel Raimond

OXFORD GRADUATE TEXTS



## And, above all

- Happy birthday, Vincent



- 60 already? I can hardly believe it.